



Spinel-trirutile microwave dielectric ceramics with high Q and excellent temperature stability based on $\text{MgO-Al}_2\text{O}_3\text{-Ta}_2\text{O}_5$ ternary systems

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ABSTRACT

$(1-x)\text{MgAl}_2\text{O}_4\text{-}x\text{MgTa}_2\text{O}_6$ composite ceramics based on the $\text{MgO-Al}_2\text{O}_3\text{-Ta}_2\text{O}_5$ pseudoternary phase diagram were prepared by the solid-state reaction. MgAl_2O_4 and MgTa_2O_6 could coexist due to their different crystal structures. MgAl_2O_4 inhibited the rapid growth of MgTa_2O_6 grains, and dense microstructures ($\rho > 95\%$) with a uniform grain size distribution was obtained, with an optimal densification temperature of 1550–1575 °C. The temperature coefficient of resonant frequency (τ_f) and quality factor ($Q \times f$) were optimized by introducing MgTa_2O_6 phases with low dielectric loss and positive τ_f . In addition, the partial solid solutions of Al^{3+} into Ta^{5+} sites resulted in loosening bonds within $[\text{Al}/\text{TaO}_6]$ octahedra and abnormally large polarizabilities, which was confirmed by the decrease in $V_{\text{Ta-O}}$ and the redshift of $A_{1g}(\text{Ta-O})$ mode. Consequently, the relative permittivity (ϵ_r) and τ_f values of $\text{MgAl}_2\text{O}_4\text{-MgTa}_2\text{O}_6$ composite ceramics were further enhanced, exceeding the predicted ones. The $0.6\text{MgAl}_2\text{O}_4\text{-}0.4\text{MgTa}_2\text{O}_6$ composition sintered at 1550 °C achieved excellent performance, with a near-zero τ_f value of 3.3 ± 1.7 ppm/°C, a low ϵ_r of 16.4 ± 0.3 and an ultra-high $Q \times f$ of $179,000 \pm 6700$ GHz @ 8.94 \pm 0.04 GHz. These findings hold promising applications in the field of 5 G/6 G high-frequency communication.

1. Introduction

With the tremendous demand for Integrated Circuits and millimeter-wave communication, microwave dielectric ceramics (MDCs) have been extensively developed for use in related microelectronic components [1–3]. To minimize inductive crosstalk and signal delay at high frequencies ($T_{\text{PD}} = \frac{\sqrt{\epsilon_r}}{c}$), a low relative permittivity ($\epsilon_r \leq 15$) is essential for MDCs [4–7]. In addition, MDCs require a high-quality factor ($Q > 10,000$ at operating frequency f_0) and a near-zero temperature coefficient of resonant frequency ($\tau_f \sim 0$) for precise frequency selectivity and temperature stability. Developing such material is complicated since the optimization of individual properties leads in opposite directions. Although lattice distortion by doping could optimize τ_f , this inevitably induces a low $Q \times f$ [8]. One effective approach involves combining two phases with opposite τ_f values to control them towards near-zero and sustain high $Q \times f$ values [9].

Spinel ceramics with the general formula AB_2O_4 , specifically M_2TiO_4 , M_2SiO_4 and MAl_2O_4 (where $\text{M} = \text{Zn, Mg}$) are promising materials for millimeter-wave devices due to their high $Q \times f$ and low ϵ_r ($Q \times f > 100,000$ GHz, $\epsilon_r = 7.5$). However, their negative τ_f (-70 ppm/°C) limits practical applications [10,11]. Previous studies have revealed the relationship between structural evolution and the improved microwave dielectric properties of MgAl_2O_4 ceramics. Chen et al. [12] highlighted the potential for achieving ultra-high intrinsic $Q \times f$ values of 394,000 GHz of MgAl_2O_4 by suppressing non-intrinsic defects. Takahashi et al. [13–16] improved the cation distribution and $Q \times f$ values of spinel solid solutions. Several other compounds, including $(1-x)\text{ZnAl}_2\text{O}_4\text{-}x\text{Mg}_2\text{TiO}_4$, $\text{MgAl}_2\text{-}x(\text{Zn}_{0.5}\text{Ti}_{0.5})_x\text{O}_4$, $(1-x)\text{MgAl}_2\text{O}_4\text{-}x\text{Mg}_2\text{TiO}_4$, $\text{MgAl}_2\text{O}_4\text{-Mg}_2\text{GeO}_4$, have also achieved satisfactory $Q \times f$ values up to about 180,000 GHz [17–20]. Because these modifications are ineffective in adjusting τ_f values, compensating phases such as TiO_2 and Sr/CaTiO_3 were added, which effectively shift the negative τ_f of MgAl_2O_4 to near

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zero. However, $Q \times f$ values of such composites are below 100,000 GHz due to the high polarization loss [21,22]. Hence, exploring novel compensating material with less dielectric loss, positive τ_f and good chemical compatibility is essential to enhance the dielectric properties of MgAl_2O_4 -based ceramics.

A previous study indicated that within the $x\text{MgO-Ta}_2\text{O}_5$ binary system, MgTa_2O_6 possesses impressive microwave dielectric properties, with a high $Q \times f$ and a positive τ_f ($Q \times f > 160,000$ GHz, $\tau_f > 30$ ppm/°C) [23]. Through the formation of MgTa_2O_6 -based solid solutions, the $Q \times f$ values could be further improved [24–26]. In addition, the coexistence of MgTa_2O_6 with MgTiO_3 or $\text{MgZrTa}_2\text{O}_8$ has been reported, allowing for control of the composites' τ_f values to near zero [27,28]. These findings suggest that MgTa_2O_6 is a potential compensating material for MgAl_2O_4 . Utilizing the thermodynamic equilibrium approach that avoids chemical reactions proves to facilitate performance optimization through composition [29]. Typically, in a binary or ternary phase diagram, two phases connected by a tie line tend to create a new equilibrium system where the chemical potential gradient difference ($\mu_A - \mu_B = 0$) is zero. In a $\text{MgO-Al}_2\text{O}_3\text{-Ta}_2\text{O}_5$ pseudoternary phase diagram, a tie line is discovered linking MgTa_2O_6 to MgAl_2O_4 . The compositions positioned along the $\text{MgTa}_2\text{O}_6\text{-MgAl}_2\text{O}_4$ tie line are investigated to potentially obtain novel composite ceramics with ultra-low dielectric loss and excellent frequency stability. The different crystal structures and adapted sintering temperatures of MgTa_2O_6 and MgAl_2O_4 could mitigate the influence of structural nonuniformity and prevent co-firing problems. Herein, the $(1-x)\text{MgAl}_2\text{O}_4\text{-}x\text{MgTa}_2\text{O}_6$ (Samples 1–6 in Fig. S1 refer to $x = 0.3, 0.4, 0.5, 0.6, 0.7, 0.8$) composite ceramics were synthesized by the solid-state reaction route. Phase compositions, microstructures and crystal structures were systematically investigated and correlated with microwave dielectric properties.

2. Experimental procedure

The high-purity powders of light MgO (Sinopharm Chemical Reagent Co., Ltd., Shanghai, China, 98.5%), Ta_2O_5 (Aladdin Reagent Co., Ltd., Shanghai, China, 99.5%) and Al_2O_3 (Sinopharm Chemical Reagent Co., Ltd., Shanghai, China, 99%) were used as raw materials. MgO was calcined at 900 °C for 2 h to remove adsorbed carbon dioxide and moisture. The pretreated raw materials were weighed according to the MgAl_2O_4 and MgTa_2O_6 stoichiometry and then charged into nylon jars with ethanol and zirconia balls for planetary ball-milling for 12 h at 200 rpm. After drying at 70 °C for 5 h and sieving, the uniformly mixed powders were calcined at 1400 °C for 4 h and 1250 °C for 6 h to synthesize MgAl_2O_4 and MgTa_2O_6 , respectively. Afterward, the as-prepared MgAl_2O_4 and MgTa_2O_6 powders were weighed in an appropriate molar ratio according to the chemical formula of $(1-x)\text{MgAl}_2\text{O}_4\text{-}x\text{MgTa}_2\text{O}_6$ ($x = 0.3, 0.4, 0.5, 0.6, 0.7, 0.8$). The mixtures were re-milled for another 12 h at the same speed of 200 rpm and then dried at 70 °C. After granulating with 5 wt% polyvinyl alcohol (PVA), the powders were pressed into cylinders (10 mm \times 6 mm) under a uniaxial pressure of 200 MPa. Finally, all samples were heat-treated at 600 °C for 2 h to remove organic residues and sintered at 1525–1600 °C for 4 h with a 5 °C/min heating rate. SEM test samples were ground and polished using varigrained metallographic abrasive paper (1000 mesh, 1500 mesh and 2000 mesh) with ethanol step by step. Subsequently, the samples were thermally etched at 50 °C below the sintering temperature for 30–60 min.

X-ray powder diffraction (D8 Advance, Bruker, Karlsruhe, Germany) with Cu K α radiation ($\lambda = 1.54060$ Å) was operated to check the phase composition. To analyze detailed information for phase fraction and structure parameters, the measured data were fitted by Rietveld refinement using the FullProf program. Scanning electron microscopy (Model SU8010, Hitachi, Japan) with energy-dispersive spectroscopy (EDS) was performed to observe the microstructure and element distribution of polished and thermally etched ceramic surfaces. SEM image analysis software (Nano Measure System) was used to count the linear

intercept of more than 100 clear grains and obtain the average grain size. The distribution histogram of grain size was also plotted using Origin software. Raman spectra were recorded by LabRAM HR Evolution spectrometer with a 532 nm excitation laser. Dielectric properties in the microwave region of $(1-x)\text{MgAl}_2\text{O}_4\text{-}x\text{MgTa}_2\text{O}_6$ ceramics were obtained using a vector network analyzer (N5234A, Agilent, USA). Among them, the Hakki–Coleman resonator method [30] was employed to obtain ϵ_r at 10–13 GHz, while the resonant cavity method assessed $Q \times f$ values at 7–10 GHz [31,32]. The resonant frequency drift determined τ_f values within a temperature range of 25–85 °C, and the calculated formula was expressed as:

$$\tau_f = \frac{f_{85^\circ\text{C}} - f_{25^\circ\text{C}}}{f_{25^\circ\text{C}}(85 - 25)} \times 10^6 (\text{ppm}/^\circ\text{C}) \quad (1)$$

3. Results and discussion

Fig. 1 illustrates the XRD patterns of $(1-x)\text{MgAl}_2\text{O}_4\text{-}x\text{MgTa}_2\text{O}_6$ ceramics sintered at 1575 °C for 4 h. The diffraction peaks are assigned to the spinel MgAl_2O_4 (ICDD No. 21–1152) and the trirutile MgTa_2O_6 (ICDD No. 32–0636). The MgTa_2O_6 peaks become stronger relative to the MgAl_2O_4 peaks as x increases, indicating that the two phases can coexist effectively. In accordance with the $\text{MgO-Ta}_2\text{O}_5$ phase diagram, Mg-rich secondary phases are inevitably generated [23], including a minor quantity of $\text{Mg}_5\text{Ta}_4\text{O}_{15}$ and $\text{Mg}_4\text{Ta}_2\text{O}_9$, as observed in the enlarged figure. As shown in Fig. 1(c, d), the Face-Centered Cubic structure with the $Fd\bar{3}m$ symmetry of MgAl_2O_4 comprises edge-sharing $[\text{AlO}_6]$ and $[\text{MgO}_4]$ polyhedra. In contrast, the trirutile structure of MgTa_2O_6 belongs to the $P4_2/mnm$ space group. All Mg^{2+} and Ta^{5+} cations are chemically coordinated, forming $[\text{Mg/TaO}_6]$ octahedra connected by O1 and O2 through a common top. The distinct crystal structures contribute to a favorable chemical compatibility between MgAl_2O_4 and MgTa_2O_6 . Nevertheless, the comparable six-fold coordination of $[\text{Al/TaO}_6]$ octahedra could potentially result in the formation of partial solid solutions and slightly alter dielectric properties.

To further investigate the phase composition and crystal structures of $(1-x)\text{MgAl}_2\text{O}_4\text{-}x\text{MgTa}_2\text{O}_6$ composite ceramics, we conducted Rietveld refinements. The fitted XRD patterns in Fig. S2 (Supplementary Information, SI) closely match the measured data points, demonstrating the reliability of the refinement results. As shown in Fig. S3, the unit cell volume of MgAl_2O_4 and MgTa_2O_6 decreases with the increase in x possibly because partial Ta^{5+} ions (ionic radius = 0.64 Å) are replaced by Al^{3+} ions (ionic radius = 0.535 Å). Notably, the mass fractions given in Table S1 (Supplementary Information, SI) reveal that as x increases, the secondary phase disappears and the actual phase contents of MgAl_2O_4 and MgTa_2O_6 approach the intended values.

Fig. 2 displays the bulk densities and relative densities of the $(1-x)\text{MgAl}_2\text{O}_4\text{-}x\text{MgTa}_2\text{O}_6$ composite ceramics sintered at various temperatures. Given its theoretical density (~ 7.816 g/cm³) surpassing that of MgAl_2O_4 (~ 3.578 g/cm³), the addition of MgTa_2O_6 results in an increase in the bulk densities of the samples. The relative densities of all samples gradually rise with increasing sintering temperature, corresponding to grain growth and fewer pores. The addition of an appropriate amount of MgTa_2O_6 improves the sintering behavior of the composite ceramics, achieving a relative density exceeding 95% at temperatures between 1550 °C and 1575 °C. However, due to over-sintering and the formation of internal pores at 1600 °C, the relative densities rapidly decline with more MgTa_2O_6 percentages, which degrades high-temperature stability and narrows the sintering temperature window.

Fig. 3 depicts the SEM images of the polished and thermally etched surfaces of $(1-x)\text{MgAl}_2\text{O}_4\text{-}x\text{MgTa}_2\text{O}_6$ ceramics ($x = 0.4, 0.8$) sintered at 1575 °C for 4 h. All samples exhibit a dense and non-porous microstructure, aligning with the result of relative density. To determine the chemical compositions of the morphologically distinct grains, the EDS analysis was performed. As analyzed in Fig. S4 (Supplementary

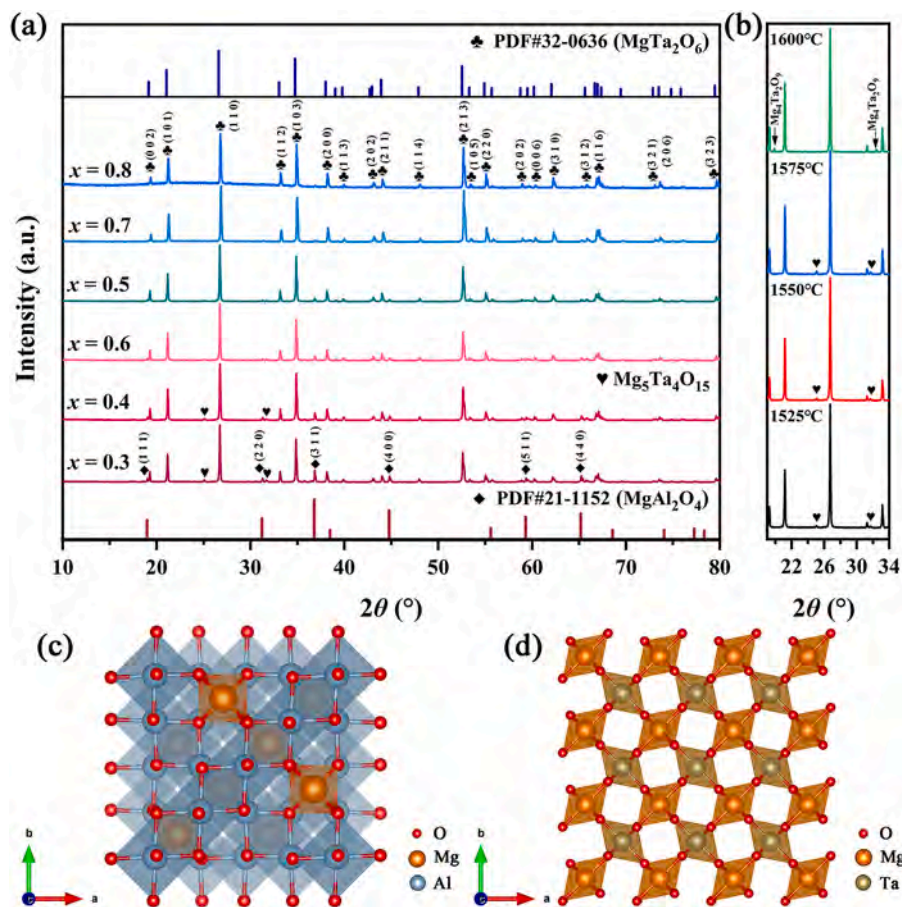


Fig. 1. (a) XRD patterns of $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ ceramics sintered at 1575°C , (b) enlarged XRD patterns of $x = 0.4$ samples sintered at different temperatures, (c) the spinel structure of MgAl_2O_4 ceramics, and (d) the rutile structure of MgTa_2O_6 ceramics.

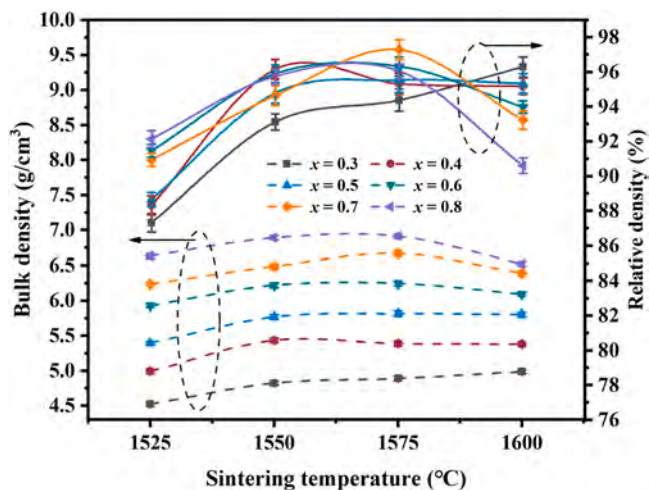


Fig. 2. Bulk densities and relative densities of the $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ ceramics ($x = 0.3 - 0.8$) as a function of sintering temperatures.

Information, SI), the equiaxial grain with the Mg to Al molar ratio of 0.54 is identified as MgAl_2O_4 . The large polygon-like grain with the Mg to Al + Ta molar ratio of 0.65 is denoted as MgTa_2O_6 . These findings collectively indicate the coexistence of MgAl_2O_4 and MgTa_2O_6 phases, with the partial solid solution of Al^{3+} into Ta^{5+} sites. Some Mg-rich phases, such as $\text{Mg}_5\text{Ta}_4\text{O}_{15}$ or $\text{Mg}_4\text{Ta}_2\text{O}_9$, can exist in parallel, possibly due to the partial solid solution and the decomposition of MgTa_2O_6 [33]. Moreover, Fig. S5 illustrates how the grain size distribution depends on

the phase fraction. Since MgAl_2O_4 plays a role in the pinning effect and inhibits the rapid growth of MgTa_2O_6 grain, a uniform grain size distribution is obtained. Regrettably, the more MgTa_2O_6 is present, the less resistance there is to grain growth, resulting in a bimodal distribution of the grain size in the $x = 0.8$ sample. Rapid grain growth and potential melting of the MgTa_2O_6 grains at temperatures above 1600°C significantly impact the high-temperature stability of the composite ceramics, leading to the formation of internal pores and a decrease in overall performance.

To reveal the inherent connection between lattice vibration and dielectric properties, Raman spectra of $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ were studied. Utilizing group theory analysis, the Raman-active vibrational modes of MgAl_2O_4 and MgTa_2O_6 are deduced from the irreducible representations of $\Gamma = A_1g + E_g + 3T_2g$ and $\Gamma = 4A_1g + 2B_1g + 4B_2g + 6E_g$, respectively [34,35]. As shown in Fig. 4, a total of 13 Raman active modes of MgTa_2O_6 are identified and those of MgAl_2O_4 disappear due to the lower intensity and peak overlaps. The modes between 118 and 330.6 cm^{-1} are assigned to Ta-O bending vibrations, including $3E_g$, B_1g , B_2g , and A_1g . The Mg-O coupled vibration generates the E_g and B_1g modes at 420.2 and 469.1 cm^{-1} , respectively. Additionally, the E_g mode ($\sim 647.5\text{ cm}^{-1}$) and the A_1g mode ($\sim 706.9\text{ cm}^{-1}$) result from the Ta-O stretching vibrations, responding sensitively to structural changes in oxygen octahedra [36,37].

Fig. S6 (Supplementary Information, SI) displays the variation in Raman shift and full width at half peak (FWHM) of the A_1g (Ta-O) mode with the x value. When the volume fractions of the MgAl_2O_4 and MgTa_2O_6 are close, the A_1g (Ta-O) mode exhibits a blueshift, attributed to the internal compressive stress and contracted $[\text{TaO}_6]$ octahedra induced by the differential thermal expansion coefficients and grain

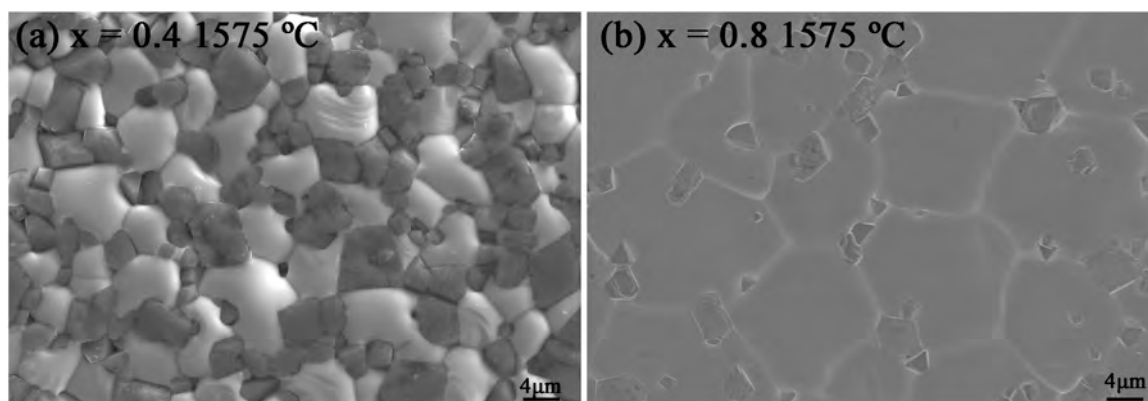


Fig. 3. SEM images of $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ ceramics with $x = 0.4$ and $x = 0.8$ sintered at 1575°C for 4 h.

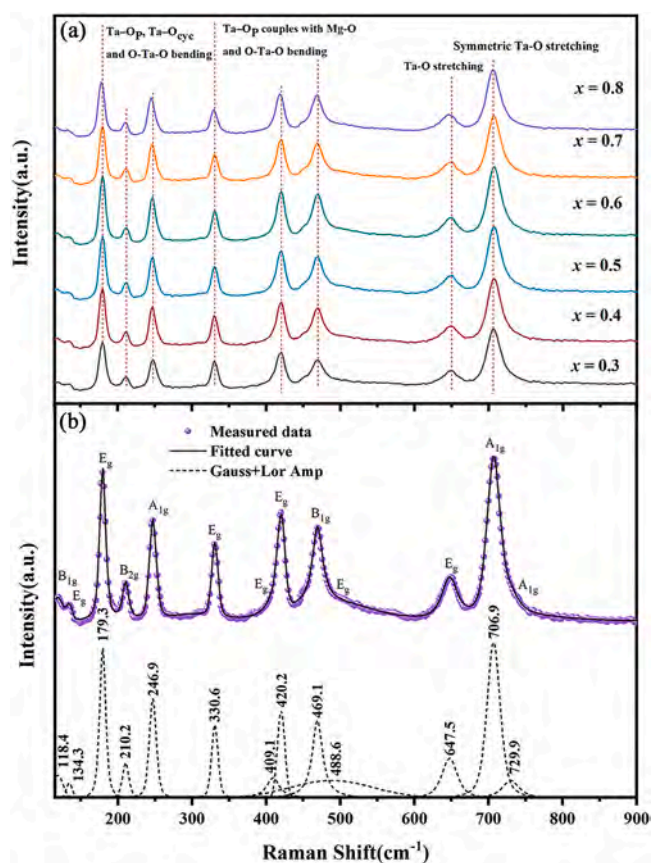


Fig. 4. (a) Raman spectra and (b) peak fitting results of $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ ($0.3 \leq x \leq 0.8$) at room temperature. *Ta-O bonds are simply bridged (Ta-O_p) or doubly bridged, forming a cycle (Ta-O_{cyc}).

growth orientations. This phenomenon may further inhibit the grain growth of MgTa_2O_6 . As x increases from 0.4 to 0.7, the redshifted $A_{1g}(\text{Ta-O})$ mode implies the weakened Ta-O bonds, corresponding to the increasing bond length detailed in Table S2. The internal stress could affect the lattice spacing and electronic properties, which enhances the anharmonic vibration and dielectric loss. Hence, a strong correlation is determined between the FWHM and the Raman shift of the $A_{1g}(\text{Ta-O})$ mode. In addition, with increasing x , the narrower bandwidth of the A_{1g} mode suggests the improved long-range ordering of the crystal structure and the reduction in the dielectric loss [33].

The variation in ϵ_r and $Q \times f$ values of the $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ composite ceramics is presented in Fig. 5. The ϵ_r exhibits a sintering

temperature dependence similar to density and increases with a reduction in porosity. The poor high-temperature stability severely degrades the performance of the $x = 0.6 - 0.8$ samples sintered at 1600°C . As x rises from 0.3 to 0.8, the ϵ_r of the composite ceramic sintered at optimal temperature increases from 13.6 ± 0.3 to 25.0 ± 0.3 . Based on the logarithmic mixing rule (Eq. S1 in Supplementary Information), the theoretical ϵ_r was calculated and compared with the measured ϵ_r . The similar variation trend between the measured and calculated values demonstrates that the high permittivity of MgTa_2O_6 is the main reason for the enhanced ϵ_r of the composite ceramic.

The factors influencing $Q \times f$ values, including porosity, phase composition, grain size distribution, and structural defects, are more complicated than those affecting relative permittivity. In Fig. 5(c), the $Q \times f$ values of the $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ ceramics increase and then decline as the sintering temperature rises, and the trend is consistent with that of relative density. The addition of MgTa_2O_6 phase with 30–60 mol% contributes to improving sintering behavior and enhancing $Q \times f$ values. Nevertheless, excessive MgTa_2O_6 leads to a decline in high-temperature stability and performance. Besides porosity, the phase composition significantly affects $Q \times f$ values of composite ceramics, as revealed in Fig. 5(d). Owing to the ultra-low dielectric loss ($Q^{-1} \approx 3.3 \times 10^{-5}$) reported in the literature for MgTa_2O_6 , the $Q \times f$ value of the $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ ceramics increases with increasing x , fluctuating around the calculated values from Eq. S2 (Supplementary Information, SI). Notably, the rapid growth of MgTa_2O_6 grains is hindered, and Al^{3+} cations partially diffuse into Ta^{5+} sites. This results in a uniform grain size distribution and improved long-range cations ordering [33], yielding high $Q \times f$ values of $179,000 \pm 6700$ GHz and $182,000 \pm 8100$ GHz in the $x = 0.4$ and $x = 0.6$ samples, respectively. The composite ceramics demonstrate superior dielectric properties in the narrow sintering interval of $1550 - 1575^\circ\text{C}$, requiring further optimization of sinterability to address the application challenges.

The variation in τ_f values with x is described in Fig. 6. The τ_f value rises from -8.2 ± 2.2 towards 28.5 ± 1.8 ppm/ $^\circ\text{C}$ with increasing x from 0.3 to 0.8. Based on the mixing rule (Eq. S3 Supplementary Information, SI), the theoretical τ_f of the composite ceramic was calculated, which displays a similar trend to the measured value. The trend with x confirms that the positive τ_f of MgTa_2O_6 plays a crucial role in optimizing τ_f values of the $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ composite ceramics. Moreover, the calculated and measured values deviate considerably, yielding a near-zero τ_f around $x = 0.4$ rather than around $x = 0.6$ theoretically. The unexpected difference may result from the structural distortion characterized by the bond distance and bond valence of Al/Ta sites ($V_{\text{Al/Ta-O}}$). According to formulas (2) and (3) [8,36], the bond valence can be calculated:

$$V_i = \sum_j V_{ij} \quad (2)$$

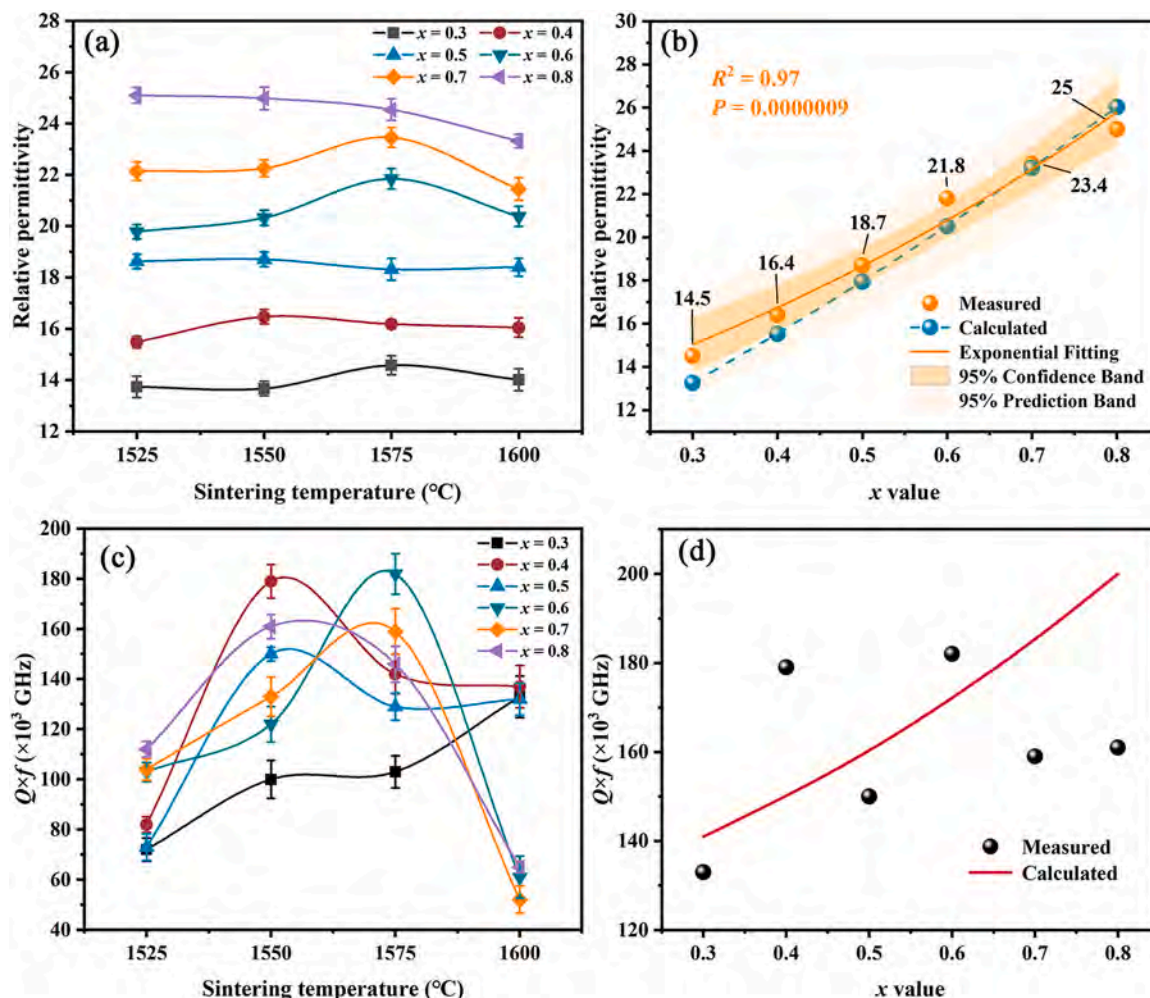


Fig. 5. The relative permittivity and $Q \times f$ values of $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ ceramics as a function of sintering temperatures and x value.

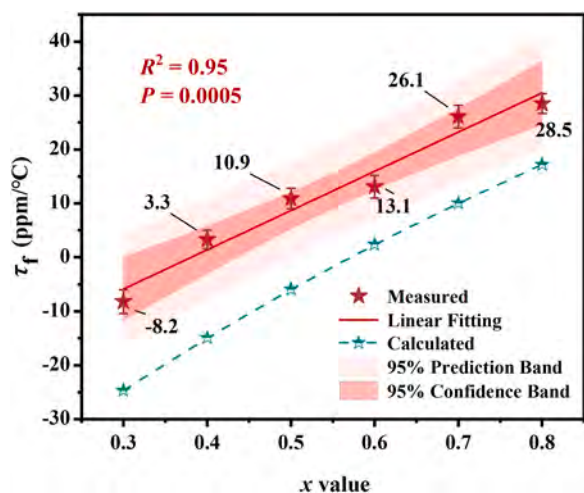


Fig. 6. The measured and calculated τ_f values of $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ ceramics sintered at optimum temperatures versus x value.

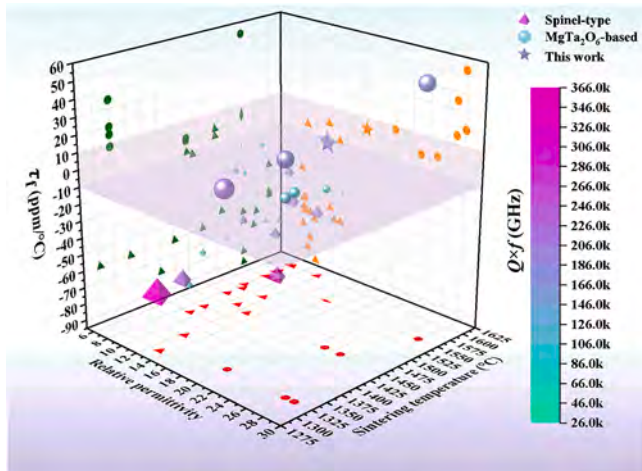
$$V_{ij} = \exp \left[\frac{R_{ij} - d_{ij}}{b} \right] \quad (3)$$

where R_{ij} is the bond valence parameter, d_{ij} is the bond length between atoms i and j , and b is a universal constant (0.37 Å). As listed in Table S2 (Supplementary Information, SI), $V_{\text{Al/Ta-O}}$ is lower than the ideal value (2.4 - 2.8 a.u. < 3 a.u. of $V_{\text{Al-O}}$ and 4.1 - 4.5 a.u. < 5 a.u. of $V_{\text{Ta-O}}$), and the $V_{\text{Ta-O}}$ shows a downward trend as x increases. The results indicate that the $[\text{Al/TaO}_6]$ octahedra becomes relatively unstable when the partial solid solution occurs, reducing the high-temperature stability of the composite ceramics. In addition, larger bond distances and thermal motions tend to result in abnormally large polarizabilities and decrease the energy required for structural restoration [8], followed by an increase in both ϵ_r and τ_f . Therefore, the measured values of ϵ_r and τ_f deviate from the calculated values. The near-zero τ_f of 3.3 ± 1.7 ppm/°C is obtained in the composition with $x = 0.4$ while maintaining a high $Q \times f$ value of $179,000 \pm 6700$ GHz and the ϵ_r of 16.4 ± 0.3 .

Compared with the other spinel and MgTa_2O_6 -based ceramics summarized in Table 1 and Fig. 7, the $(1-x)\text{MgAl}_2\text{O}_4-x\text{MgTa}_2\text{O}_6$ composite ceramics achieve the synergistic optimization for $Q \times f$ and τ_f , offering high-performance dielectric ceramics for 5 G microwave applications. Understanding the phase diagram for the preparation of composite ceramics could initiate a new direction in expanding microwave dielectric ceramic systems with excellent performances.

Table 1Comparison of sintering temperature and microwave dielectric properties of typical spinel-type and MgTa₂O₆-based ceramics.

Compounds (or methods)	S.T. (°C)	ϵ_r	$Q \times f$ (GHz)	τ_f (ppm/°C)	Ref.
MgAl ₂ O ₄	1600/5 h	7.8	85,100	-59.2	[38]
ZnAl ₂ O ₄	1600/5 h	8.5	93,300	-60	[15]
Zn _{0.4} Al _{1.6} O ₄ (molten salt)	1600/5 h	8.2	202,468	-68	[13]
Mg _{0.4} Al _{1.6} O ₄ (molten salt)	1600/50 h	7.5	232,301	-60	[14]
MgAl ₂ O ₄ + 6.4 mol.%LiF	1575/8 h	8.36	99,900	-61.57	[39]
(Mg _{0.25} Zn _{0.75})Al ₂ O ₄	1600/5 h	8.4	222,600	-52	[15]
(Mg _{0.75} Ni _{0.25})Al ₂ O ₄	1510/3 h	8.21	130,000	-53.5	[40]
(Mg _{0.8} Co _{0.2})Al ₂ O ₄	1475/6 h	8.46	49,300	-60	[41]
(Mg _{0.96} Cu _{0.04})Al ₂ O ₄	1550/4 h	8.28	72,800	-59	[42]
Mg _{0.4} Al _{1.2} Ga _{0.4} O ₄	1600/5 h	11.8	191,340	-54	[16]
ZnAl _{1.9} (Zn _{0.5} Ti _{0.5}) _{0.1} O ₄	1400	9.1	115,800	-78	[43]
MgAl _{1.94} (Mg _{0.5} Ti _{0.5}) _{0.06} O ₄	1425/8 h	9.1	98,000	-61.3	[44]
MgAl _{1.5} (Zn _{0.5} Ti _{0.5}) _{0.5} O ₄	1550	9.86	263,900	-92	[18]
MgAl _{1.8} (Li _{1/3} Ti _{2/3}) _{0.2} O ₄	1550	8.78	62,300	-85	[45]
MgAl _{1.88} (Zn _{0.5} Ti _{0.5}) _{0.12} O ₄	1500	8.72	42,036	-5	[18]
0.79ZnAl ₂ O ₄ -0.21(2MO-TiO ₂)M=Co, Mg, Mn	1400–1550	9.6–9.9	23,530–160,800	-66–63	[46]
0.1MgAl ₂ O ₄ -0.9Mg ₂ TiO ₄	1350	12.36	236,600	-61	[19]
Mg ₂ GeO ₄ -MgAl ₂ O ₄	1600	8.0	150,000	-34	[20]
0.7Mg ₄ Nb ₂ O ₉ -0.15ZnAl ₂ O ₄ -0.15TiO ₂	1300	13.1	366,000	-60.8	[33]
90 wt%(0.75ZnAl ₂ O ₄ -0.25TiO ₂)-10 wt%MgTiO ₃	1450	12.99	69,245	-9.5	[21]
0.75MgAl ₂ O ₄ -0.25TiO ₂	1460	11.03	105,400	-12	[22]
MgTa _{1.92} Sb _{0.08} O ₆	1325	27	109,000	15	[24]
Mg _{0.94} Mn _{0.06} Ta ₂ O ₆	1325	28	105,000	19.5	[25]
Mg _{0.94} Ni _{0.06} Ta ₂ O ₆	1325	27	173,000	35	[26]
2MgO-Ta ₂ O ₅ + 0.5 wt%B ₂ O ₃	1325	19.9	211,000	8	[23]
0.7MgTiO ₃ -0.3MgTa ₂ O ₆	1450	23	81,000	-2	[27]
0.25MgZrTa ₂ O ₈ -0.75MgTa ₂ O ₆	1450	24.88	26,823	-0.5	[28]
0.7MgAl ₂ O ₄ -0.3MgTa ₂ O ₆	1600	14.0 ± 0.4	133,000 ± 8300	-8.2 ± 2.2	This work
0.6MgAl ₂ O ₄ -0.4MgTa ₂ O ₆	1550	16.4 ± 0.3	179,000 ± 6700	3.3 ± 1.7	This work
0.5MgAl ₂ O ₄ -0.5MgTa ₂ O ₆	1550	18.7 ± 0.3	150,000 ± 2700	10.9 ± 1.9	This work

**Fig. 7.** Summary of relative permittivity, $Q \times f$ values, τ_f values and sintering temperatures for spinel-type and MgTa₂O₆-based ceramics.

4. Conclusions

The phase composition, microstructure and microwave dielectric properties of (1-x)MgAl₂O₄-xMgTa₂O₆ composite ceramics were systematically investigated. The XRD and EDS analysis revealed MgAl₂O₄ and MgTa₂O₆ as the main crystalline phases along with the partial solution of Al³⁺ into Ta⁵⁺ sites. The $Q \times f$ and τ_f values of the composite ceramics were optimized due to the low dielectric loss and positive τ_f value of MgTa₂O₆. Specifically, excellent dielectric properties were obtained at dense samples with $x = 0.3 - 0.5$ sintered at 1550 - 1575 °C: a series of ϵ_r of 14.0 ± 0.4 to 18.7 ± 0.3 , high $Q \times f$ values of $133,000 \pm 8300$ to $182,000 \pm 8100$ GHz and near-zero τ_f of -8.2 ± 2.2 to 10.9 ± 1.9 ppm/°C. The improved microstructure with porosity-free and uniform grain size distribution correlated the MgAl₂O₄ phase to the

Zener pinning effect. Moreover, the lower V_{Ta-O} and the redshift of the A_{1g}(Ta-O) mode suggested the weakening of the bond strength within [TaO₆] octahedra, resulting in abnormally large polarizabilities and a further increase in both ϵ_r and τ_f . This work directed a practical processing route to fabricate competitive candidate materials for 5 G/6 G millimeter-wave communications.

CRediT authorship contribution statement

Jian Li: Conceptualization, Methodology, Investigation, Formal analysis, Writing – original draft, Writing – review & editing. **Xiaohan Zhang:** Data curation, Investigation, Validation. **Jia Liu:** Supervision, Writing – review & editing. **Qingxuan Zhou:** Data curation, Investigation. **Haitao Wu:** Methodology, Writing – review & editing, Supervision, Resources, Funding acquisition. **Yuanyuan Zhou:** Methodology, Supervision. **Yang Wang:** Supervision, Writing – review & editing. **Wei Sun:** Supervision, Formal analysis. **Yanxiang Jiang:** Formal analysis. **Yongning Han:** Data curation, Validation. **Zhuoqun Han:** Supervision. **Zhicheng Zhao:** Supervision. **Futian Liu:** Methodology, Visualization, Resources, Supervision, Funding acquisition. **Yongcui Zhang:** Supervision. **Yingying Wang:** Supervision. **Ling Li:** Project administration, Supervision, Investigation, Resources, Funding acquisition. **Walther Glaubbitt:** Supervision, Writing – review & editing.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A. Supporting information

Supplementary data associated with this article can be found in the online version at doi:10.1016/j.jeurceramsoc.2024.01.017.

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